



उत्तराखण्ड मुक्त विश्वविद्यालय, हल्द्वानी (नैनीताल)

M.A./M.Sc. Mathematics ASSIGNMENT-FIRST YEAR

Last date of Submission: 15/05/2014

(जमा करने की अन्तिम तिथि: 15/05/2014.)

Course Title: Differential Geometry and Tensors

Course Code: - M.A./M.Sc. MAT 504

Year: 2013-14

Maximum Marks: 40

Section 'A' contains 08 short answer type questions of 5 marks each. Learners are required to answers 4 questions only. Answers of short answer-type questions must be restricted to 250 words approximately.

भाग क में आठ लघु उत्तरीय प्रश्न दिये गये हैं इनमें से केवल चार प्रश्नों के उत्तर देने हैं। प्रत्येक प्रश्न के लिए पांच अंक निर्धारित हैं तथा प्रत्येक प्रश्न का उत्तर 250 शब्दों से अधिक नहीं होना चाहिए।

निम्न की संक्षेप में चर्चा कीजिए :

1- Write the condition for three point contact of a curve and a surface.

2- Find the radix of curvature and torsion of a helix

$$X = a \cos \theta, y = a \sin \theta, Z = a \theta \tan x$$

3- Preure that the distance between corresponding points of two curves is constant.

4- Find the envelope of the plane

$$lx + my + nz = 0 \text{ where } a^2 + b^2 + c^2 = 0$$

5- Compute the fundamental magnitudes for the surface.

$$r = (4 \cos \vartheta, \vartheta \sin \vartheta, f \cos \vartheta + c \vartheta)$$

6- Define Conjugate directions at a given point (u, ϑ) on a surface $r = r(u, \vartheta)$

7- Show than the contraction of the onter product of the tensors A^p and B_q is an invariant.

8- Show that $\frac{\partial A^r}{\partial x^s}$ is not a tensor even though A_p is a covariant tensor of rank one.

Section 'B' contains 04 long answer-type questions of 10 marks each. Learners are required to answers 02 questions only.

भाग ख में चार दीर्घ उत्तरीय प्रश्न दिये गये हैं इनमें से केवल दो प्रश्नों के उत्तर देने हैं। प्रत्येक प्रश्न के लिए दस अंक निर्धारित हैं ।

- 1- Show that the great circles on a sphere are geodesic.
- 2- Show that the number of independent components of the covariant curvature tensor in a space of N – dimension is $\frac{N^2}{12}$

3- Prove that every point on a cone or cylinder is a parabolic point

4- Prove that

$$H N_1 = M r_1 - L r_2$$

