



UTTARAKHAND OPEN UNIVERSITY, HALDWANI (NAINITAL)
उत्तराखंड मुक्त विश्वविद्यालय, हल्द्वानी(नैनीताल)

M.A./ M.Sc. Mathematics
ASSIGNMENT- FIRST YEAR

Last Date of Submission: 15 May जमा करने की अन्तिम तिथि: 15 मई

Cosurse Title: Mechanics

Course code: MAT 505

Year: 2012-13

Maximum Marks : 40

Section 'A'

भाग क

Attempt any 04 questions. Each carry 05 marks.

1. A rough uniform board of mass m and length $2a$ rests on smooth horizontal plane, and a body, of mass M , walks on it from one end to the other. Show that the distance through which the board moves in this time is $2 ma/m+n$.
2. Show that the centres of suspension and oscillation are convertible.
3. An equilateral triangular lamina is rotating in its plane with uniform angular velocity about an axis through one vertex. If this vertex is released and one of the other vertices fixed. Show that the new angular velocity is $1/5$ of the former value.
4. A particle of mass m moves in a force field of potential V . Write the Hamiltonian.
5. A uniform sphere rolls down in inclined plane, rough enough to prevent any sliding. Find distance described in time t .
6. Set up Lagrangian for a simple pendulum.
7. If a point moves along a circle with constant speed, prove that its angular velocity about any point on the circle is half of that about the centre.
8. A heavy circular disc is revolving in a horizontal plane about its centre which is fixed. An insect, of mass $1/n^{\text{th}}$ that of the disc walk from the centre along a radius and then flies away. Show that the final angular velocity is $n/n+2$ time the original angular velocity of the disc.

Section 'B'

भाग ख

Section 'B' contains 04 long answer-type questions of 10 marks each. Learners are required to answer 02 questions only.

1. Find the equation of continuity.

2. A top is executing steady motion, with its axis inclined at a constant angle α to the vertical and precessional velocity ω . Show that motion is stable.
3. A uniform rod of mass $5m$ and length $2a$, turns freely about one end which is fixed, to its other extremity is attached one end of a light string, of length $2a$, which carries at its other end a particle of mass m , show that the periods of the small oscillations in a vertical plane are the same as those of simple pendulum of length $2a/3$ and $20a/7$.
4. A uniform rod, of mass $3m$ and length $2l$ has its middle point fixed and a mass m attached at one extremity. The rod when in horizontal position is set rotating about a vertical axis through its centre with angular velocity equal to $\sqrt{2ng/l}$, show that the heavy end of the rod will fall till the inclination of the rod to the vertical is $\cos^{-1} [\sqrt{n^2+1} - n]$ and will then rise again.